



ASTR-6000 Seminar
COLLAGE: Coronal Heating,
Solar Wind, & Space Weather

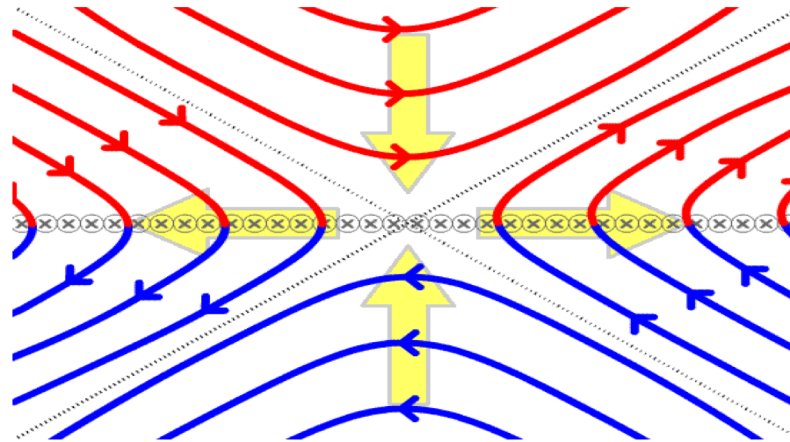
February 10, 2022

Coronal heating:
reconnection & nanoflares
(another whirlwind tour)

Dr. Steven R. Cranmer
Dr. Thomas E. Berger

Outline

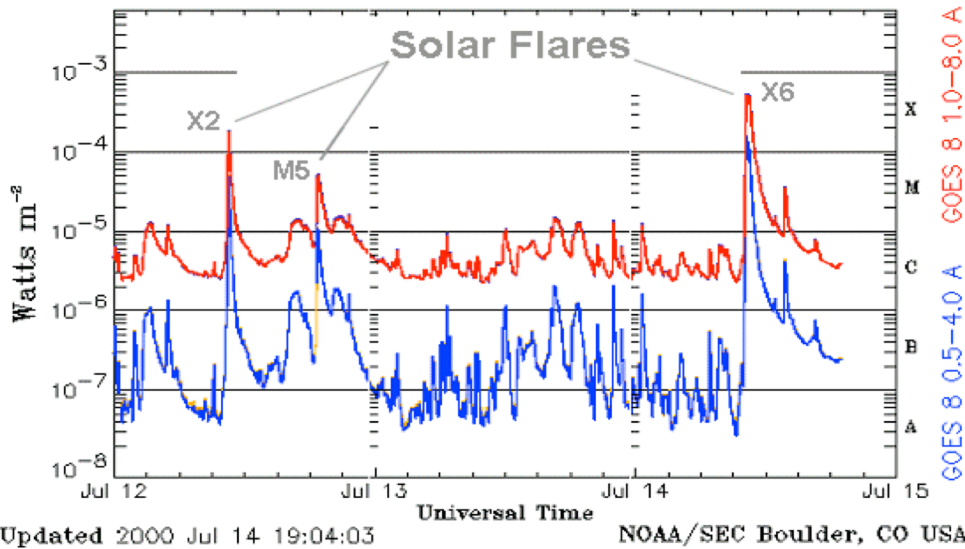
1. Observations (and cartoons!) of reconnection sites on the Sun
2. Overview of magnetic reconnection: how much does it heat?



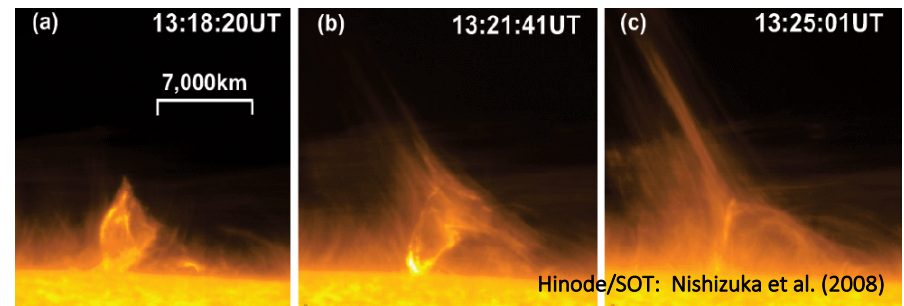
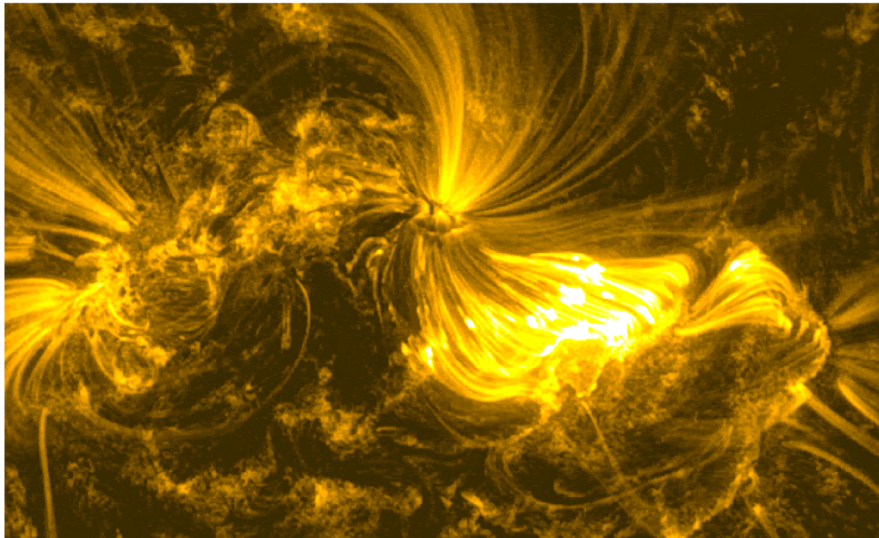
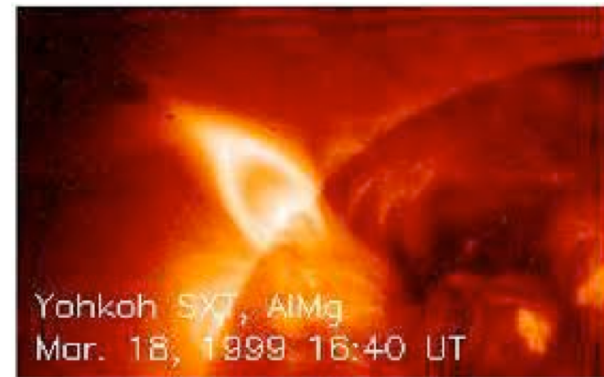
3. How is MHD turbulence relevant to all this...?

(1) *Solar observations of reconnection sites*

GOES Xray Flux (5 minute data)



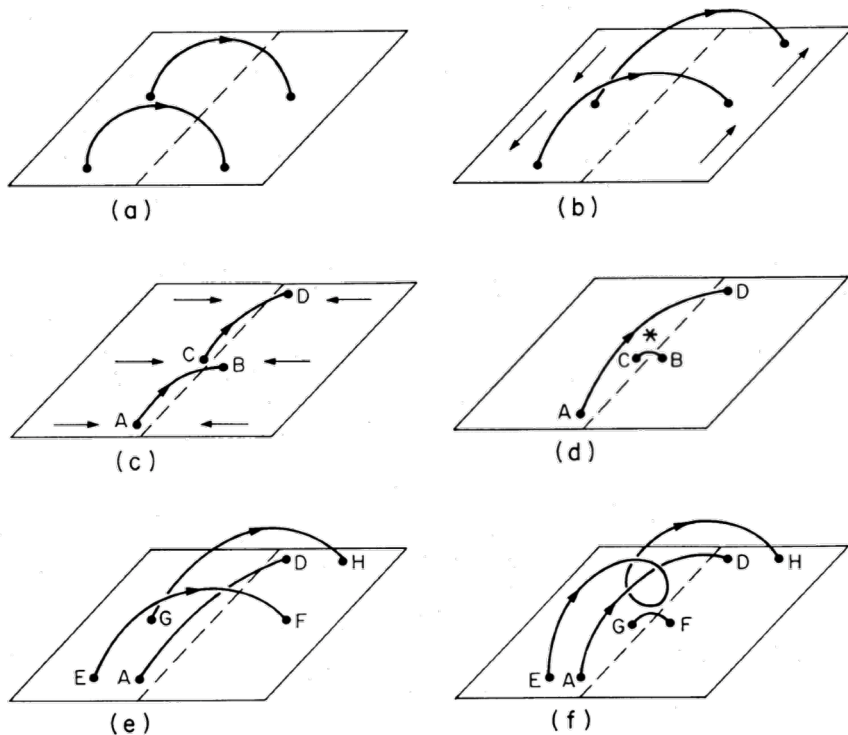
- This isn't a class about **solar flares!**
- However, if the idea is that coronal heating comes from a sum over many discrete/impulsive energy release events, we do need to look in that direction...



(1) *Solar observations of reconnection sites*

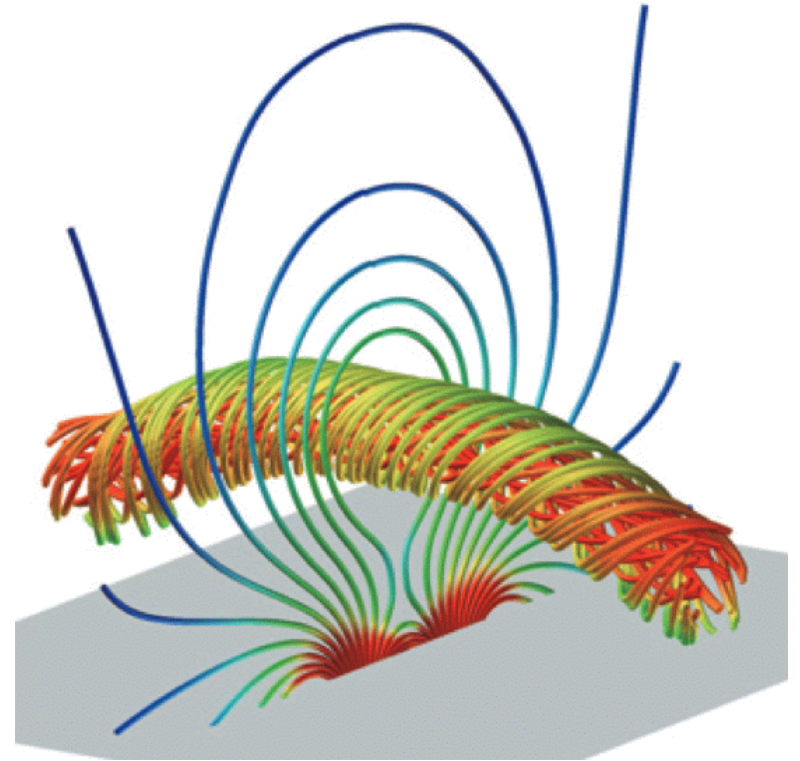
Cartoons! <https://www.astro.gla.ac.uk/cartoons/>

Twisted fields can build up as a result of shear motions on the surface
(van Ballegooijen & Martens 1989)



Formation of flux ropes & filaments . . .

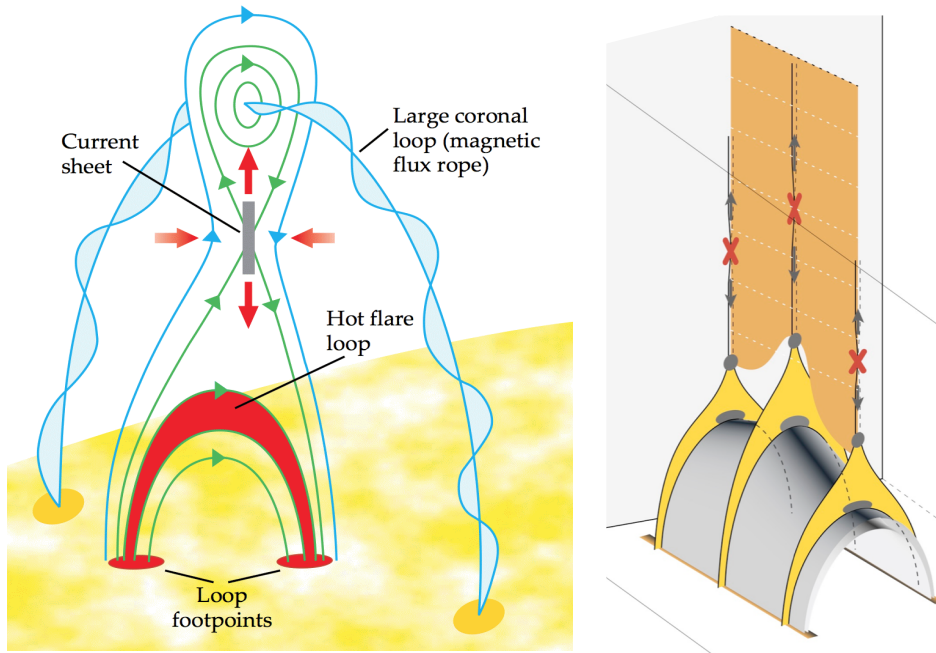
Overlying magnetic field has strong tension... wants to hold everything down.



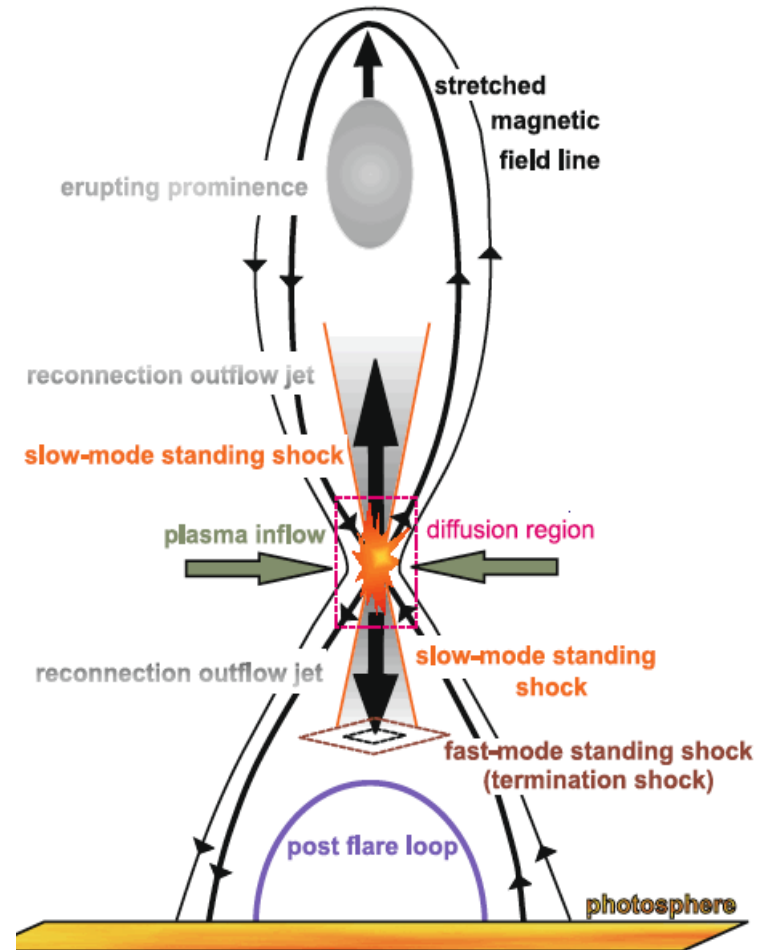
Oppositely pointed magnetic field lines are often pushed together at the coronal base.



(1) *Solar observations of reconnection sites*

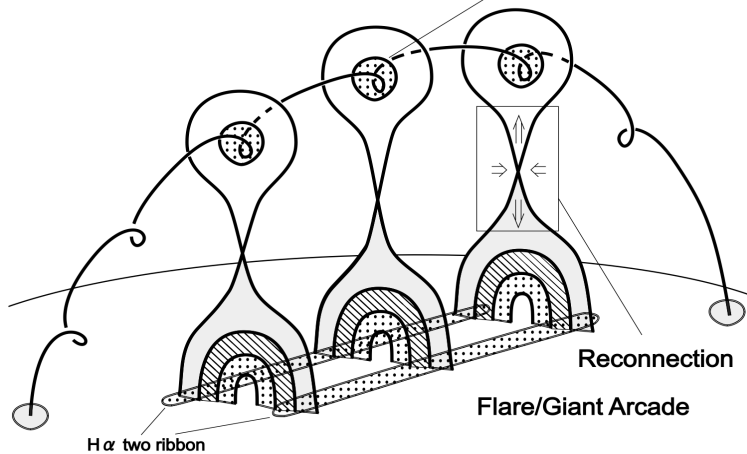


A “standard” picture of solar flares & CMEs has evolved over the years...



Coronal Mass Ejection

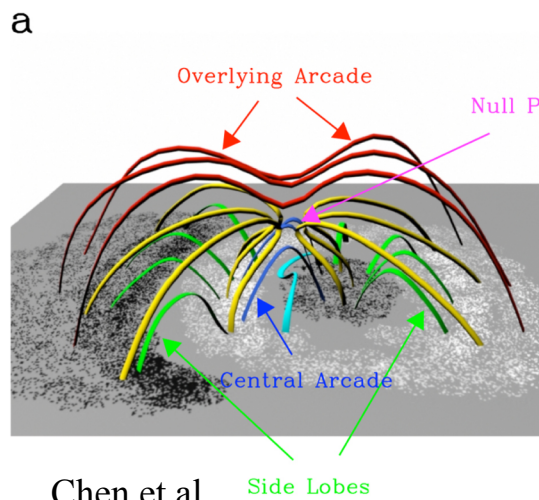
Erupting Filament



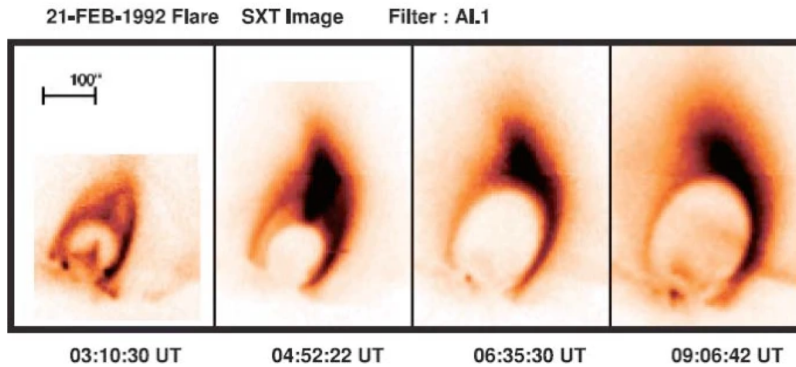
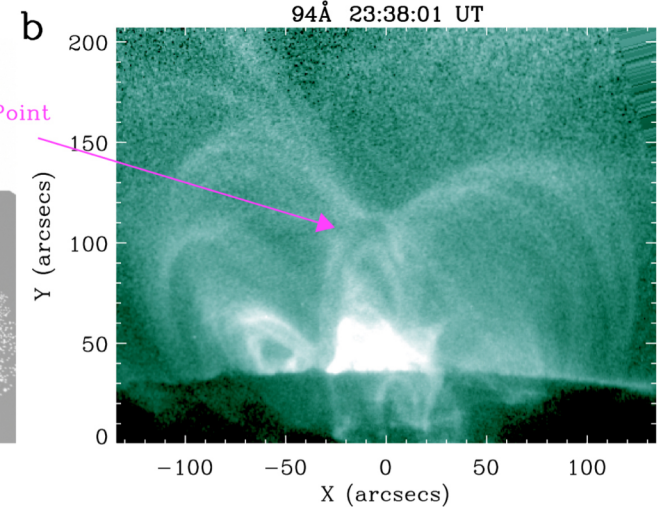
(1) *Solar observations of reconnection sites*

Decades of **observations** tend to support the basic picture of magnetic reconnection at the core of solar eruptive events...

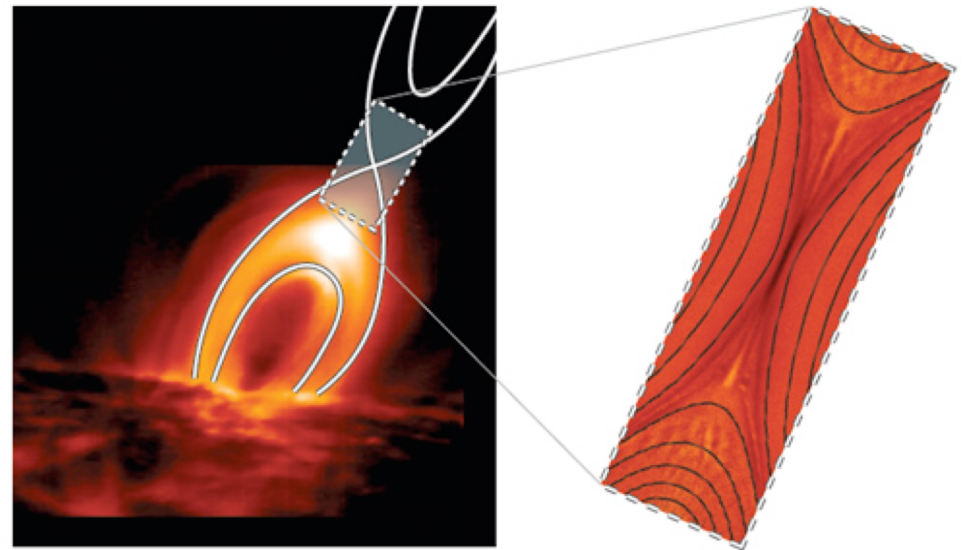
but there's huge variety amongst events...



Chen et al. (2016)



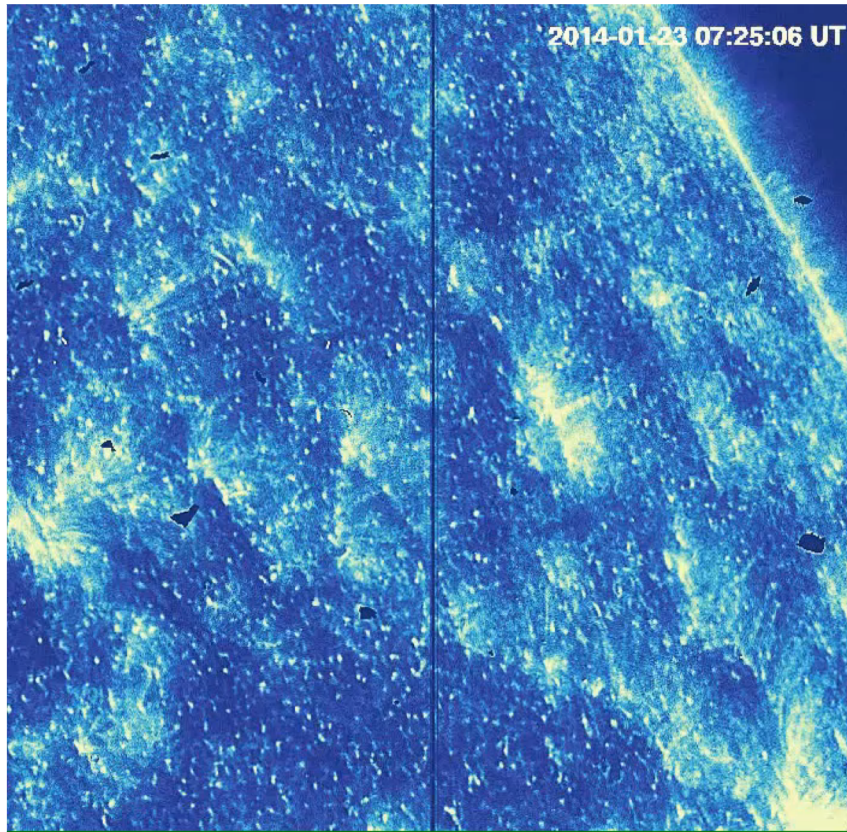
Shibata & Magara (2011)



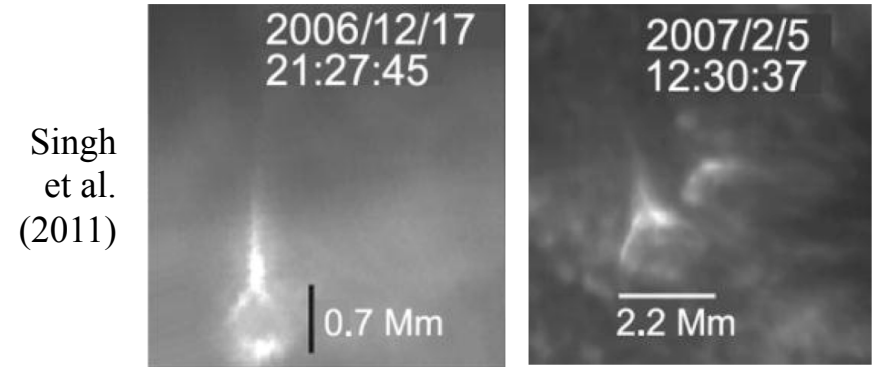
Burch & Drake (2009)

(1) *Solar observations of reconnection sites*

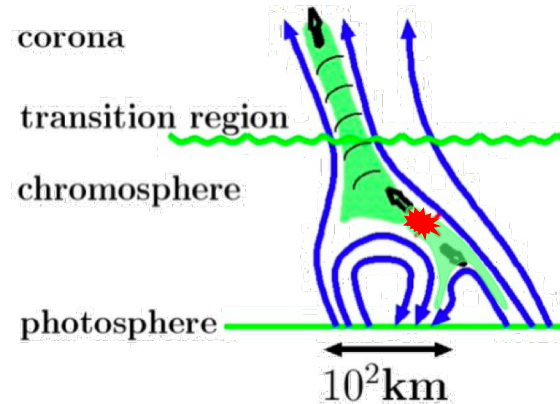
Even down to the **smallest scales** (in the chromosphere), there seems to be some kind of reconnection that drives impulsive events. Spicules, tadpoles, “anemone jets,” EUV & X-ray microflares, etc.



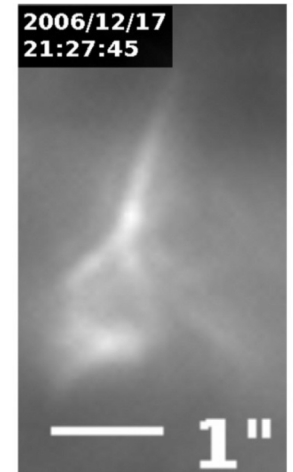
Tian et al. (2014)



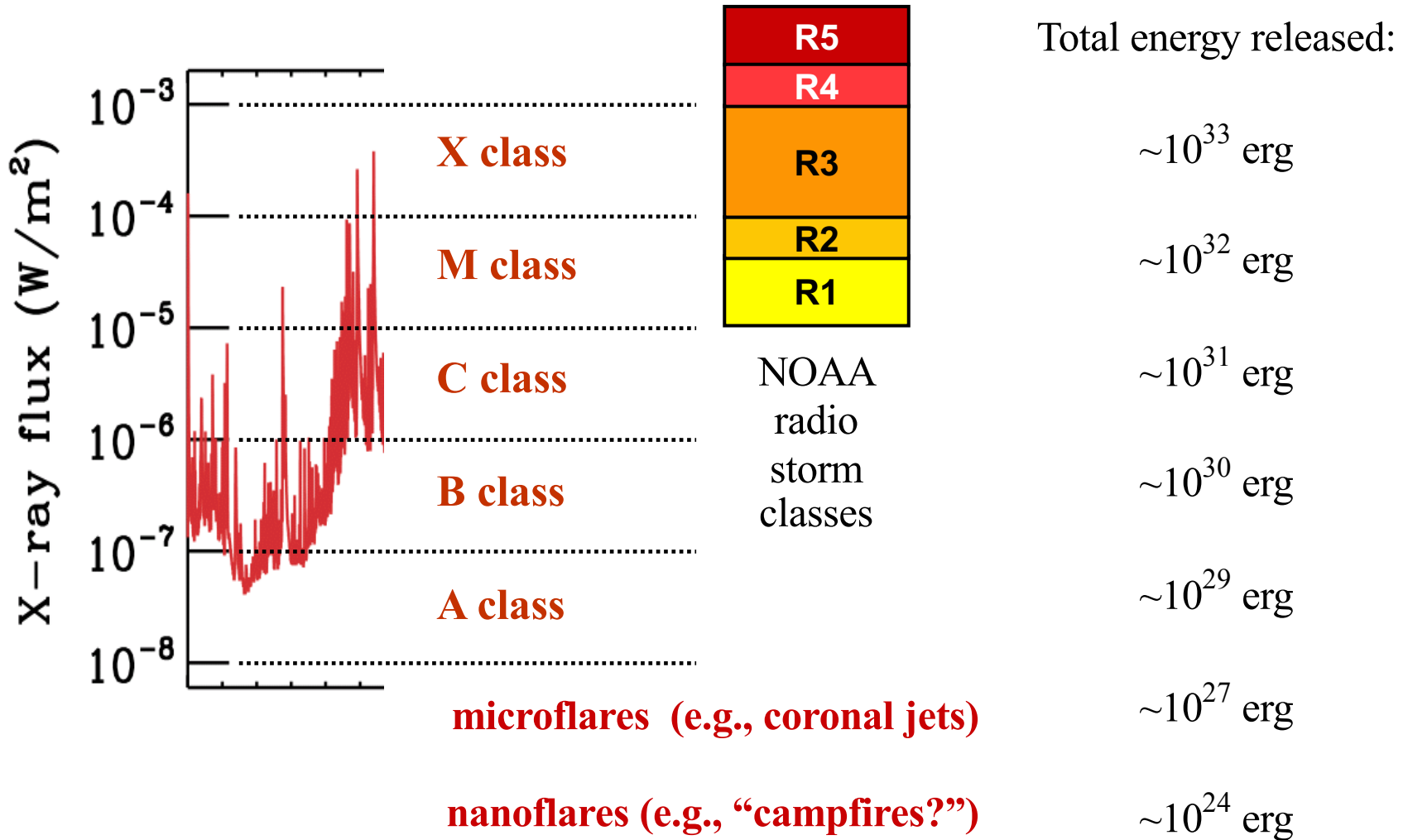
Singh et al. (2011)



Shibata et al. (2008)



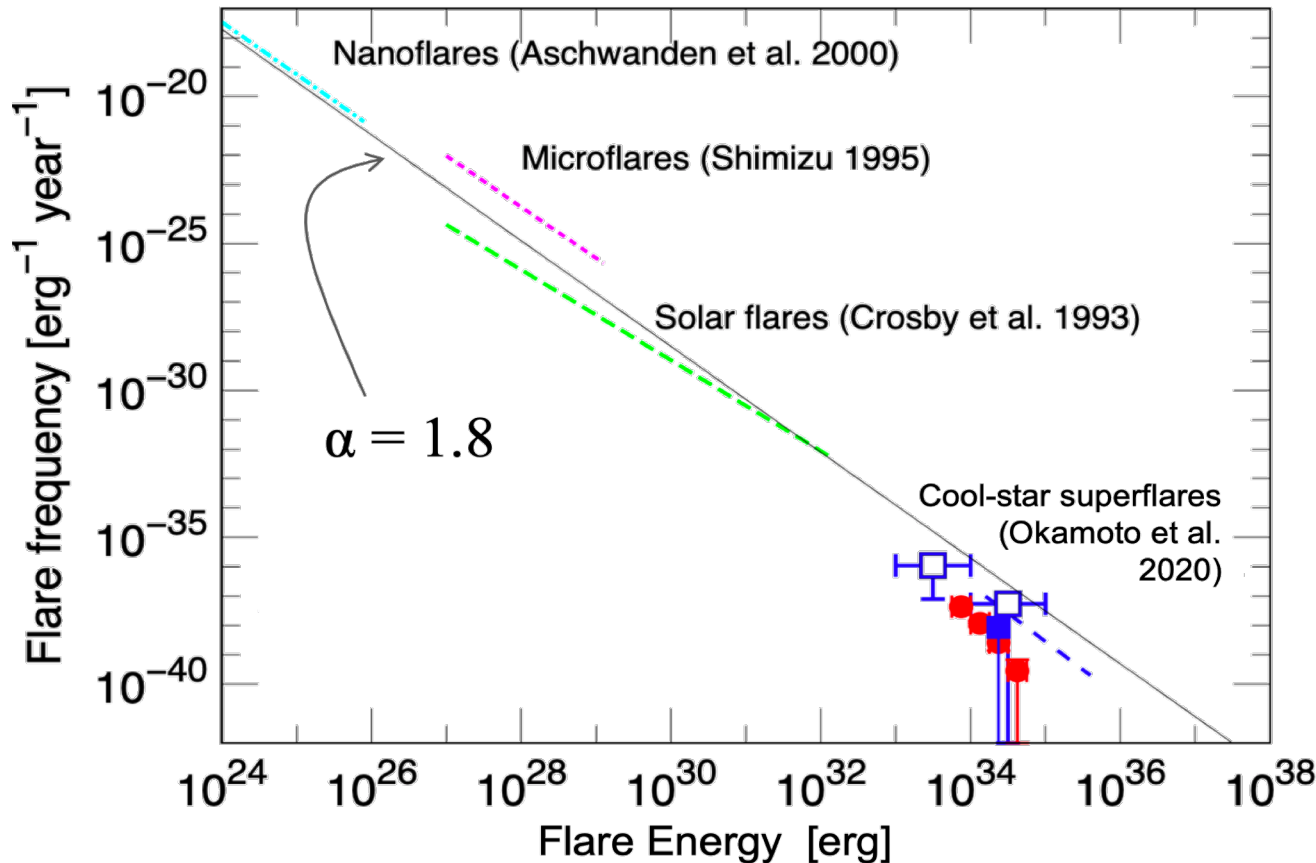
(1) *Solar observations of reconnection sites*



(1) *Solar observations of reconnection sites*

It's been known that {numbers of events} vs. {energy} is a power-law distribution... but Hudson (1991, *Solar Phys*, 133, 357) pointed out the importance of the slope...

$N(E) \propto E^{-\alpha}$ if $\begin{cases} \alpha > 2 \\ \alpha < 2 \end{cases}$ the total is dominated by the $\begin{cases} \text{smallest} \\ \text{largest} \end{cases}$ events.



but the error bars
(not shown!) are
still large...

and systematic
effects may be
obscuring the
smallest events!

(2) *Overview of magnetic reconnection*

- Let us first introduce a useful dimensionless quantity, the **Lundquist number**:

$$S = \frac{V_A L}{D_B} \sim \frac{V_A L}{v_{\text{th}} \ell_{\text{mfp}}}$$

typical speeds & length scales of macro-scale MHD flows

typical magnetic diffusion coefficient (i.e., resistive diffusivity) characterizing random-walk speeds & lengths



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- Some use the symbol η for the diffusion coefficient, but I prefer using η for the “actual” **electrical resistivity** (and σ for electrical conductivity):

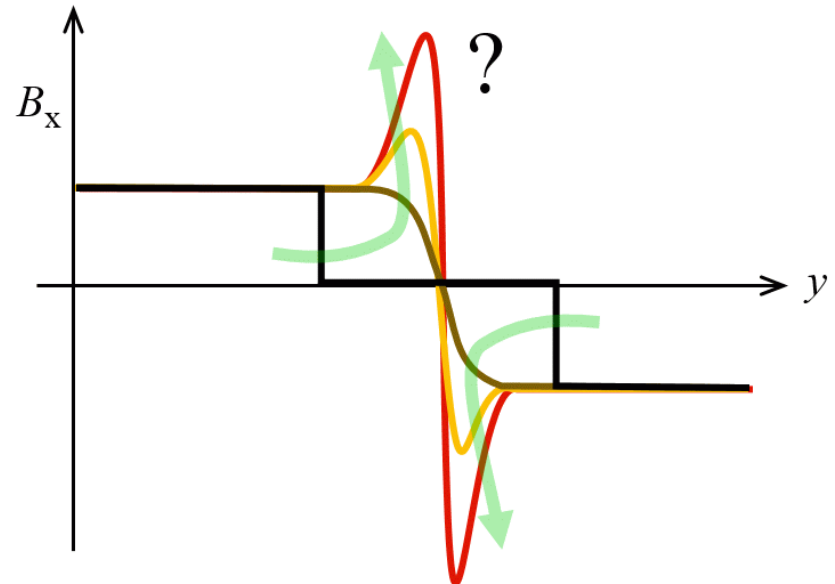
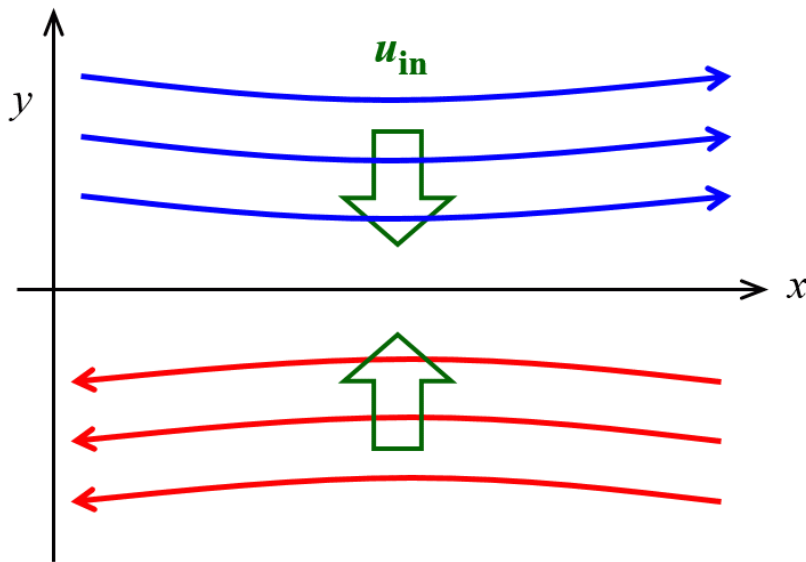
$$\mathbf{E} = \eta \mathbf{J} \qquad D_B = \frac{c^2 \eta}{4\pi} = \frac{c^2}{4\pi \sigma}$$

- Most of the coronal volume (along with most astrophysical plasmas) has $S \gg 1$ (often exceeding $\sim 10^{12}$), which means resistivity *shouldn't* be important.

(2) *Overview of magnetic reconnection*

- However, sometimes the field gets twisted up into complex topologies, with small length scales L .
- In such regions S is no longer $\gg 1$.
- If we want to study what happens when oppositely directed fields are pushed together, we're forced to take resistivity seriously.
- However, what if there was no resistivity? Pushing together perfectly “frozen-in” field lines would lead to a continual build-up... a log-jam...

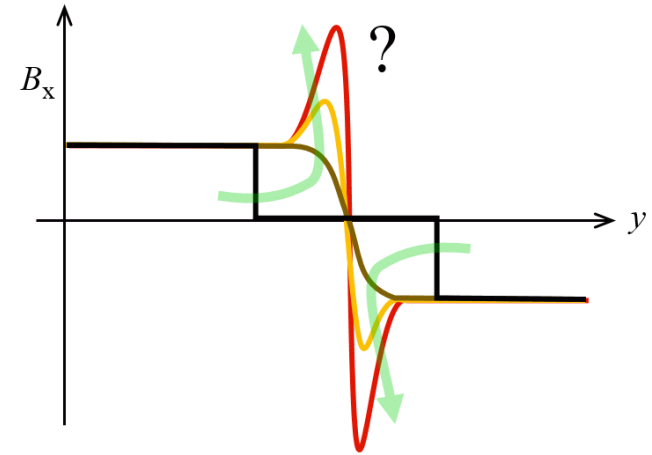
$$S = \frac{V_A L}{D_B}$$



(2) *Overview of magnetic reconnection*

- How to prevent a continuous build-up over time?
- The **resistive term** in the magnetic induction equation causes magnetic energy to diffuse... especially if there are sharp gradients!

$$\frac{\partial \mathbf{B}}{\partial t} = \nabla \times (\mathbf{u} \times \mathbf{B}) + D_B \nabla^2 \mathbf{B}$$



- Let's look for a **steady-state** between buildup & diffusion.
- Define the thickness of the reconnection region (in y) as δ . As fields build up, δ gets smaller. Also, define u_{in} as the speed at which fields are pushed together.
- Eventually, we'll reach a point where they balance...

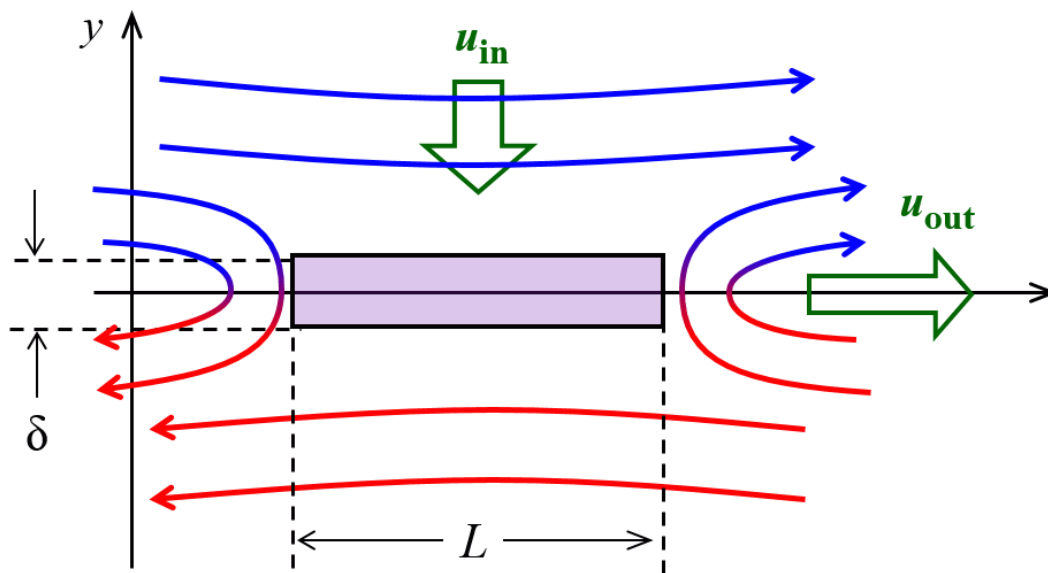
$$\frac{u_{\text{in}} \delta}{D_B} \approx 1 \quad \implies \quad \delta \approx \frac{D_B}{u_{\text{in}}}$$

- This is the point at which diffusion balances buildup. Magnetic energy is converted to heat at a continuous rate.

(2) *Overview of magnetic reconnection*

- We still don't know how the corona determines δ or u_{in} .
- The next steps are still not universally agreed upon; it's still a very active field of research.
- Let's go over the original (Sweet & Parker 1957) theory, then talk about how more recent research is in the process of improving it.
- Treat the **diffusion region** as 2D and rectangular...

$$\delta \approx \frac{D_B}{u_{in}}$$



Things we know:

- B (strength of inflowing magnetic field)
- L (length scale of the reconnection region parallel to \mathbf{B})
- ρ (mass density, assume constant everywhere)

Things we don't know:

- u_{in} , u_{out} , δ

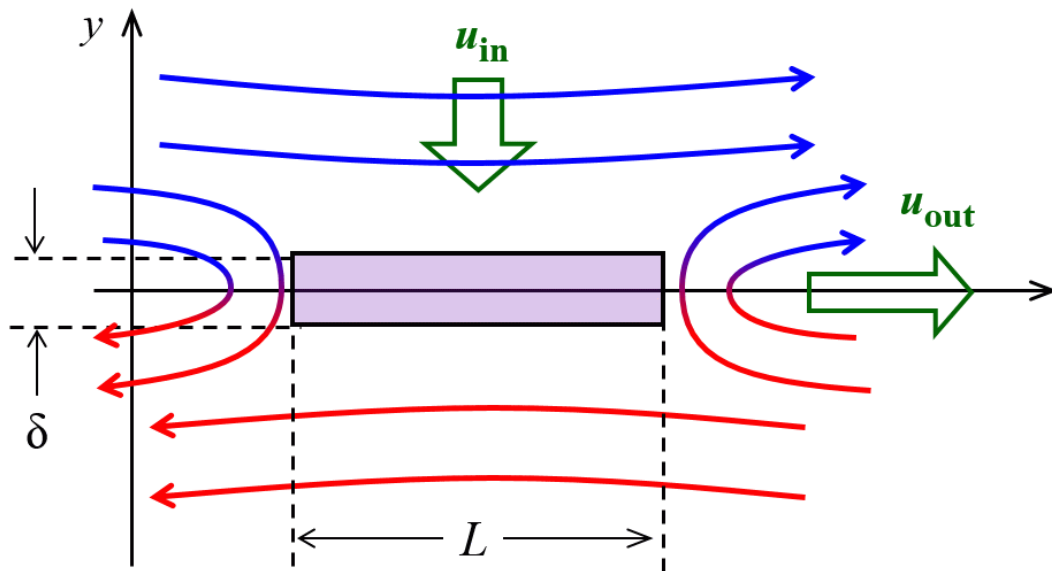


(2) Overview of magnetic reconnection

- To fully specify u_{in} , u_{out} , and δ , we need two more conditions:
- **Mass conservation:** if it's a steady state, then the total mass coming in must balance the total mass going out, in proportion to the dimensions,

$$\rho u_{\text{in}} L \approx \rho u_{\text{out}} \delta$$

Thus, the reconnection region is kind of like a **toothpaste tube** being compressed gently along its long axis, with the toothpaste jetting out forcefully along its short axis:



$$\frac{u_{\text{out}}}{u_{\text{in}}} \approx \frac{L}{\delta} \gg 1$$

(2) *Overview of magnetic reconnection*

- Lastly, there's **energy conservation**.
- Going in: assume motions are so slow that it's dominated by magnetic energy.
- Going out: B-field has been mostly cancelled; the “jets” are mostly kinetic energy.

\mathcal{E} = volume \times energy density, so

$$\begin{aligned}\mathcal{E}_{\text{in}} &= \Delta x \Delta y \Delta z U_B & \mathcal{E}_{\text{out}} &= \Delta x \Delta y \Delta z U_K \\ &= L (u_{\text{in}} \Delta t) \Delta z \left(\frac{B^2}{8\pi} \right) & &= (u_{\text{out}} \Delta t) \delta \Delta z \left(\frac{1}{2} \rho u_{\text{out}}^2 \right)\end{aligned}$$

If $\mathcal{E}_{\text{in}} = \mathcal{E}_{\text{out}}$, then $u_{\text{out}} = \frac{B}{\sqrt{4\pi\rho}} = V_A$ (the Alfvén speed) .

- In more realistic models, $\mathcal{E}_{\text{in}} \neq \mathcal{E}_{\text{out}}$ since *some* energy must go into heating up the diffusion region, and we can't totally ignore the kinetic (in) & magnetic (out) parts.

(2) *Overview of magnetic reconnection*

- We can now solve 3 equations for 3 unknowns...

$$\begin{aligned} u_{\text{in}} &= \frac{u_{\text{out}} \delta}{L} && \text{(from mass conservation)} \\ &= \frac{V_A (D_B / u_{\text{in}})}{L} && \text{(from energy conservation \& } R_m \approx 1 \text{ in box)} \end{aligned}$$

and some additional algebra, in combination with the definition of the Lundquist number, gives

$$u_{\text{in}}^2 = \frac{V_A^2}{S} \quad \text{where recall that} \quad S = \frac{V_A L}{D_B}$$

- Thus, the Sweet-Parker result for the reconnection Alfvénic Mach number (sometimes called the “dimensionless reconnection rate”) is:

$$\mathcal{M}_A = \frac{u_{\text{in}}}{V_A} = \frac{\delta}{L} = \frac{1}{\sqrt{S}} \sim 10^{-6}$$

- In the solar corona: $S \approx 10^{12}$. . . $V_A \approx 1000$ km/s . . . so $u_{\text{in}} \approx 0.001$ km/s ?

(2) *Overview of magnetic reconnection*

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- This doesn't make sense. It's too slow.
- A typical flare-producing region, with a size of about 1–10 Mm, “processes” the active-region B-field over a finite time...

$$\Delta t = \frac{\ell}{u_{\text{in}}} \approx \frac{1-10 \text{ Mm}}{0.01 \text{ km/s}} = 10^5 \text{ to } 10^6 \text{ s} \quad (\text{days/weeks})$$

(2) *Overview of magnetic reconnection*

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- However, observed flares last only 5–10 minutes! **The real u_{in} must be faster!**
- Observations, simulations, and some lab experiments now show that reconnection in MHD plasmas tends to occur with a narrow allowed range of

$$\mathcal{M}_A \approx 0.01 \text{ to } 0.1$$

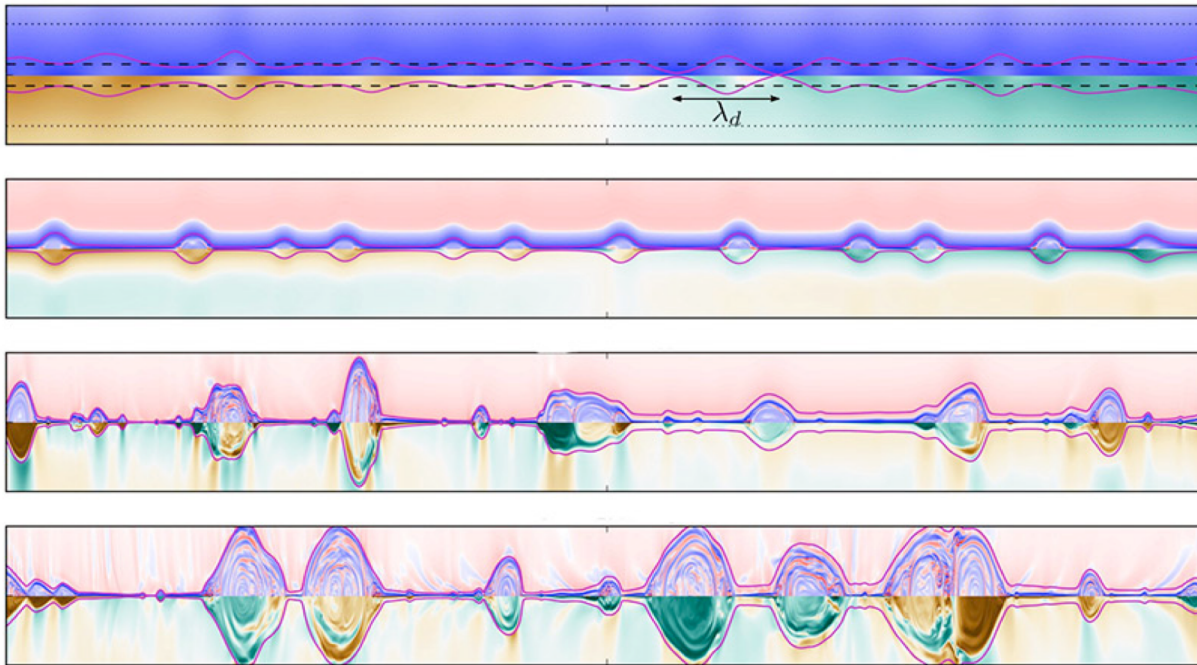


(2) *Overview of magnetic reconnection*

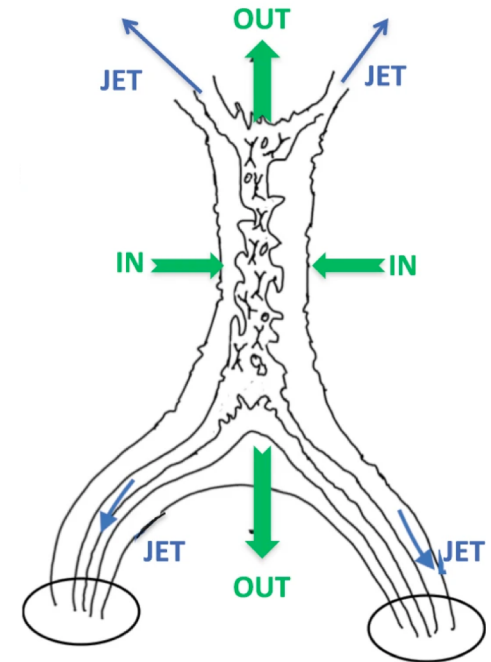
How does the universe get around the constraints of Sweet-Parker theory? It's still a topic of active research, with ~ 3 main avenues of study...

- 1. Plasmoid Instabilities:** The thin diffusion region is unstable to the spontaneous growth of small magnetic “islands.” Chaotic (fractal?) eddies produce extra diffusion:

larger $D_B \longrightarrow$ smaller effective $S \longrightarrow$ faster u_{in} !



Huang et al. (2017)

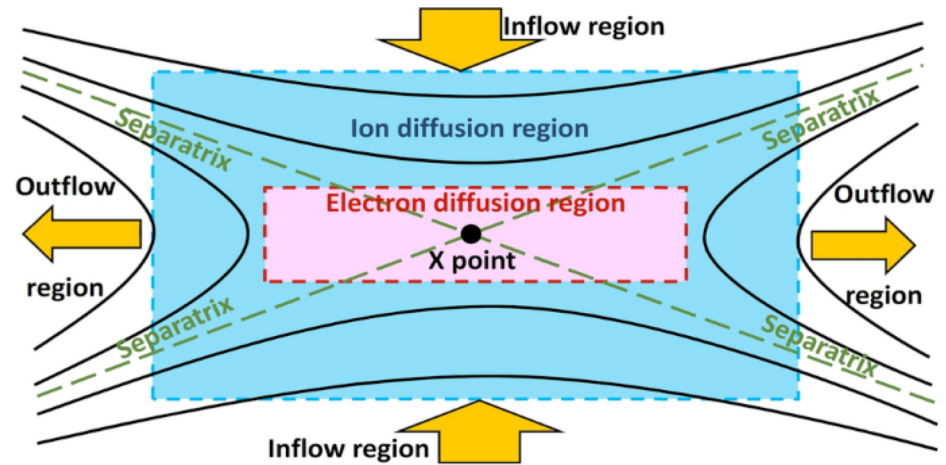


Cairns et al. (2018)

(2) Overview of magnetic reconnection

2. **Hall Effect:** If the diffusion region is forced to be smaller than particle Larmor radii, then non-MHD collisionless effects can take over.

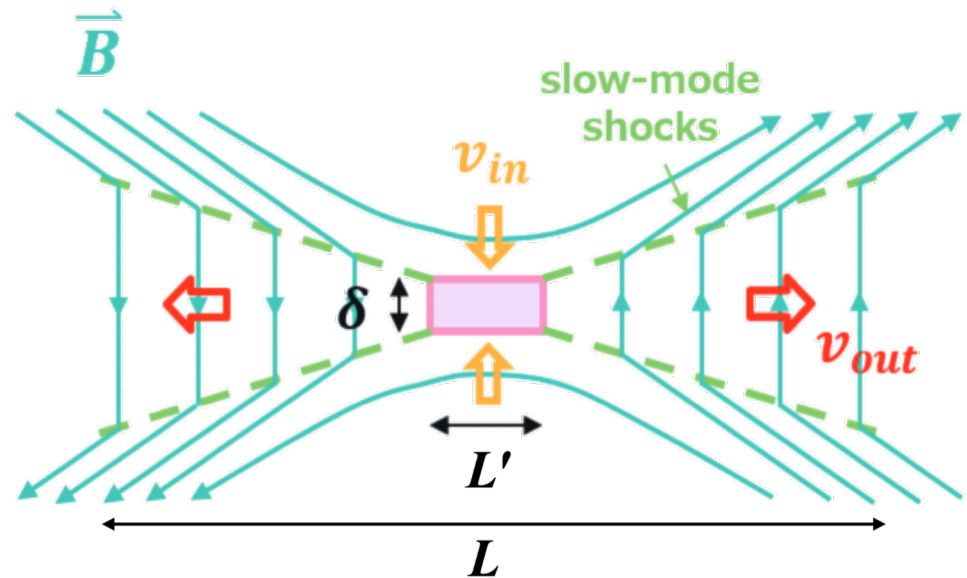
(electron scales \ll ion scales)



3. **Petschek reconnection:** Maybe not all flows must pass through the diffusion region. Petschek proposed a model with oblique MHD shocks to help “process” some of the flow.

$$\mathcal{M}_A = \frac{u_{in}}{V_A} \approx \frac{1}{\ln S}$$

(not as tiny as Sweet-Parker!)

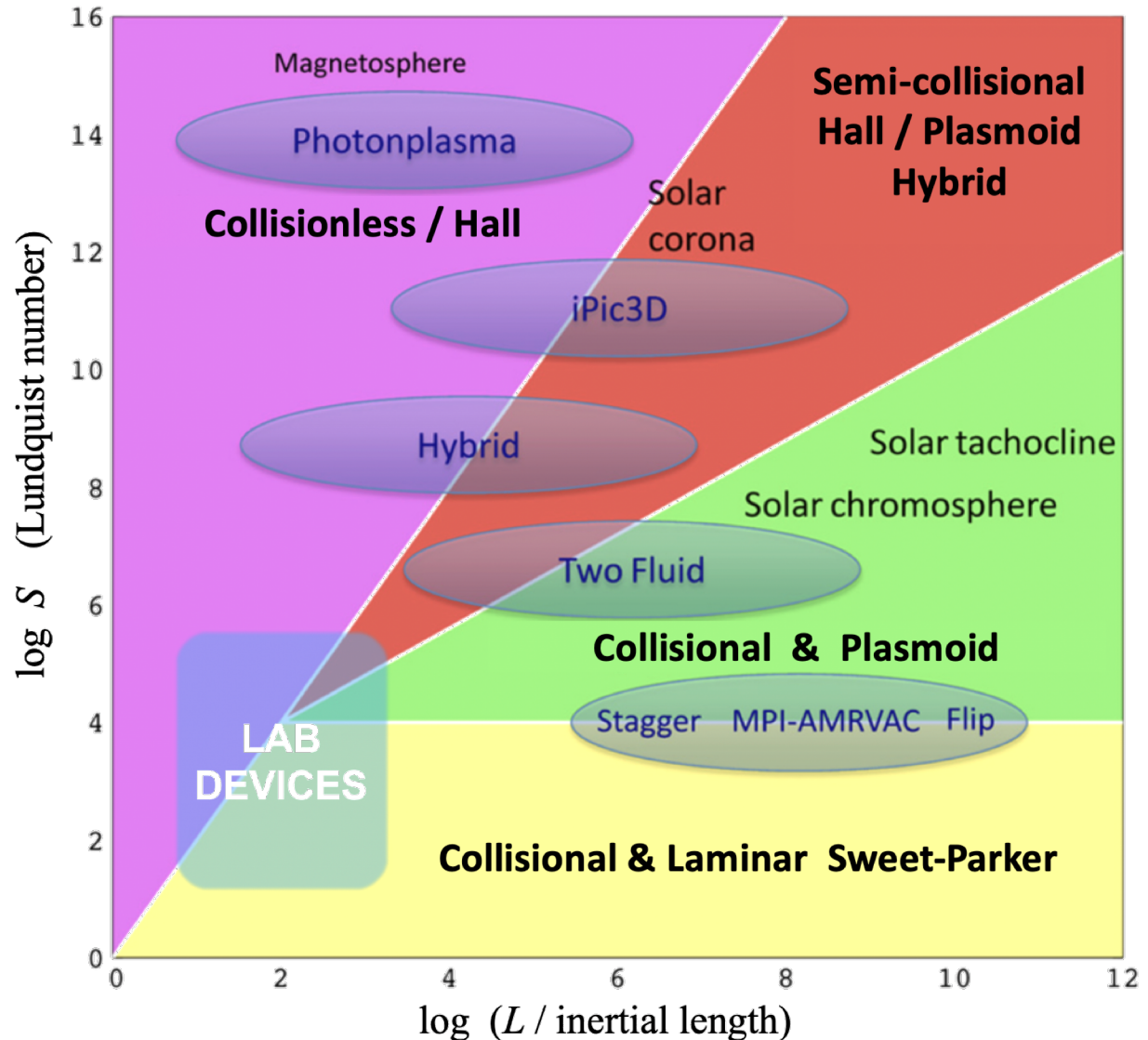


(2) Overview of magnetic reconnection

Theorists have fleshed out a kind of “phase diagram” for reconnection modes, illustrating the main regimes and (fuzzy) boundaries

(Lapenta et al. 2013, *J. Space Weather and Space Climate*, 3, A05)

Observers still find the Petschek model useful... especially for cases where *in situ* instruments fly right through the reconnection regions!

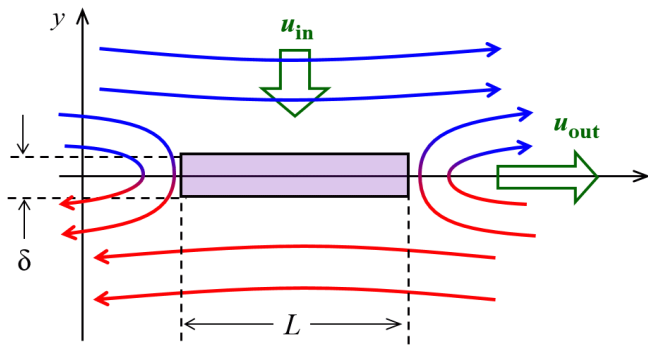


(2) *Overview of magnetic reconnection*

- One more (pretty important) question to ask about reconnection regions:
How much actual **energy (i.e., heating)** can we get out of one?

(2) Overview of magnetic reconnection

- One more (pretty important) question to ask about reconnection regions:
How much actual **energy (i.e., heating)** can we get out of one?
- The diffusion region is often called a **current sheet**... for good reason...



\mathbf{B} points mostly along x , but varies along y .
That counts as a nonzero curl!

$$\mathbf{J} = \frac{c}{4\pi} \nabla \times \mathbf{B} \quad \Rightarrow \quad J_z \sim \frac{c B_x}{4\pi \delta}$$

- If magnetic energy is dissipated & turned into heat, then

$$Q_{\text{heat}} = \mathbf{J} \cdot \mathbf{E} = J_z E_z = \eta J_z^2 \Rightarrow = \frac{u_{\text{in}} B^2}{4\pi \delta}$$

- Thus, if the event occurs over time Δt , and in a volume $V = L^2 \delta$, then the energy is:

$$\mathcal{E} = Q_{\text{heat}} V \Delta t = \frac{B^2}{4\pi} L^2 V_A \mathcal{M}_A \Delta t$$



(2) *Overview of magnetic reconnection*

$$\mathcal{E} = Q_{\text{heat}} V \Delta t = \frac{B^2}{4\pi} L^2 V_A \mathcal{M}_A \Delta t$$

- For typical solar corona regions...

$$\mathcal{E} \approx 10^{30} \text{ erg} \left(\frac{B}{1000 \text{ G}} \right)^2 \left(\frac{L}{1 \text{ Mm}} \right)^2 \left(\frac{V_A}{1000 \text{ km/s}} \right) \left(\frac{\mathcal{M}_A}{0.1} \right) \left(\frac{\Delta t}{100 \text{ s}} \right)$$

Try a small,
barely resolvable
“campfire:”

$$\left. \begin{array}{l} B \sim 100 \text{ G} \\ L \sim 0.1'' \sim 70 \text{ km} \\ \Delta t \sim 10 \text{ s} \end{array} \right\} \rightarrow \mathcal{E} \approx 4 \times 10^{24} \text{ erg} \text{ (“nanoflare”)}$$

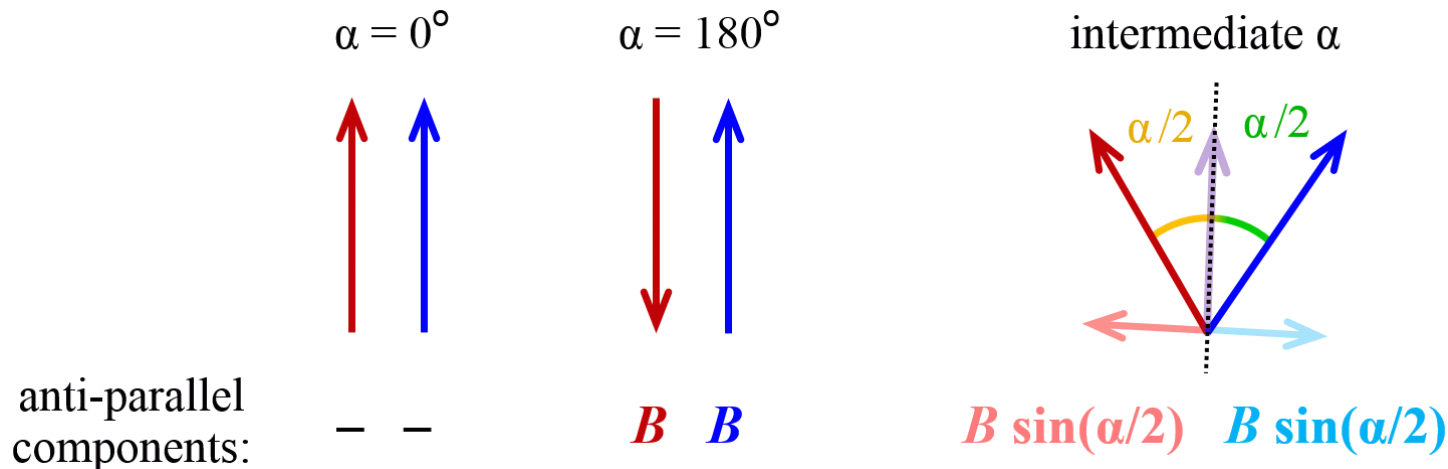
Try something
pretty massive:

$$\left. \begin{array}{l} B \sim 5000 \text{ G} \\ L \sim 30 \text{ Mm} \\ \Delta t \sim 100 \text{ s} \end{array} \right\} \rightarrow \mathcal{E} \approx 10^{34} \text{ erg} \text{ (>X10 superflare!)}$$

(2) *Overview of magnetic reconnection*

$$\mathcal{E} = Q_{\text{heat}} V \Delta t = \frac{B^2}{4\pi} L^2 V_A \mathcal{M}_A \Delta t$$

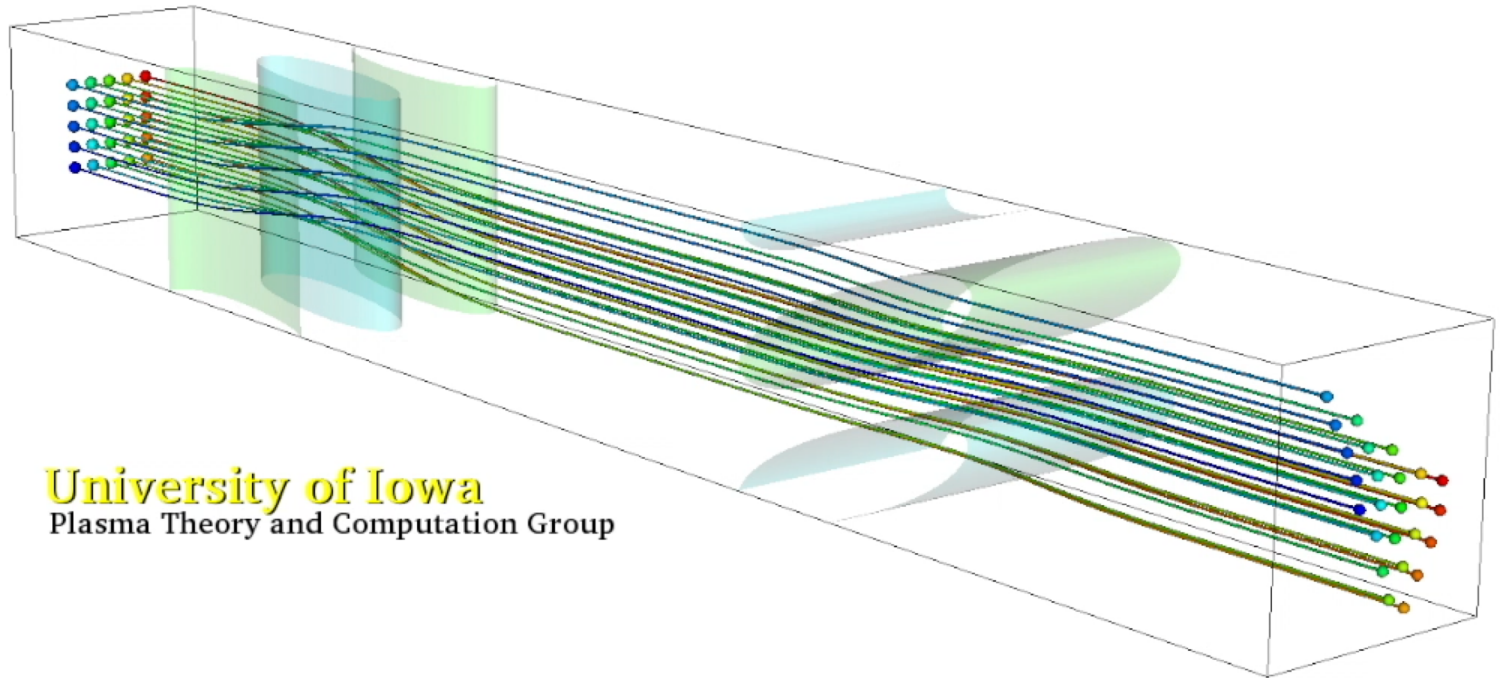
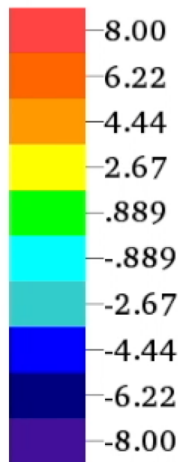
- Two final wrinkles:
- If the fields on either side are **asymmetric**, simulations show that it's fine to replace B^2 by $B_1 B_2$
- If the fields on either side aren't exactly anti-parallel (i.e., if there's a common **"guide field"** between them), one can just use the anti-parallel components:



(3) *MHD turbulence and reconnection*

- Unlike hydrodynamic turbulence, when the background \mathbf{B} -field is strong, the turbulent “eddies” take the form of counter-propagating Alfvén wave packets.
- When packets collide, nonlinear terms in MHD equations generate higher harmonics.
- Kraichnan (1965) found cascade occurs only when there is “power” in both directions...

Current density, j_z



University of Iowa
Plasma Theory and Computation Group

(3) *MHD turbulence and reconnection*

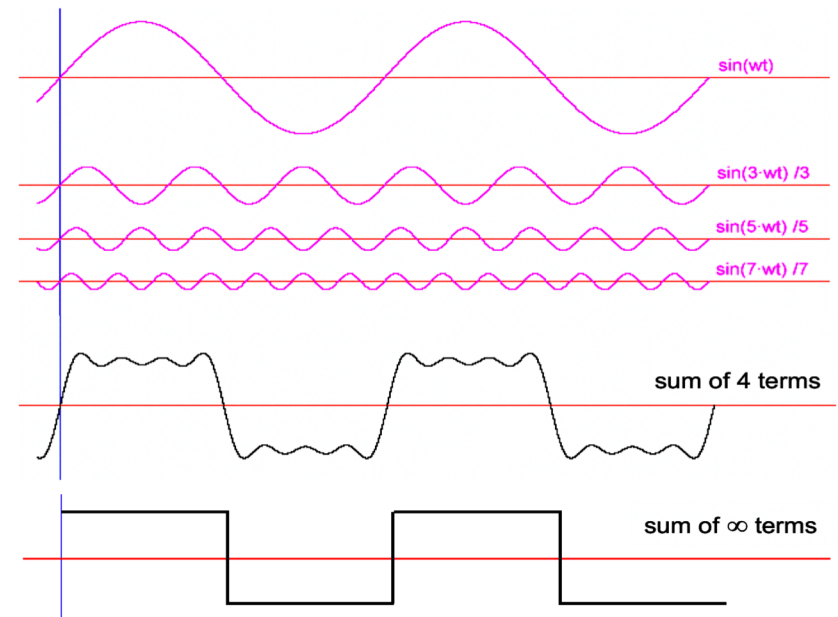
- Because magnetic fields have **tension**, most of the cascade happens perpendicular to the background field. (It's easier to shuffle dried spaghetti than it is to bend it...)

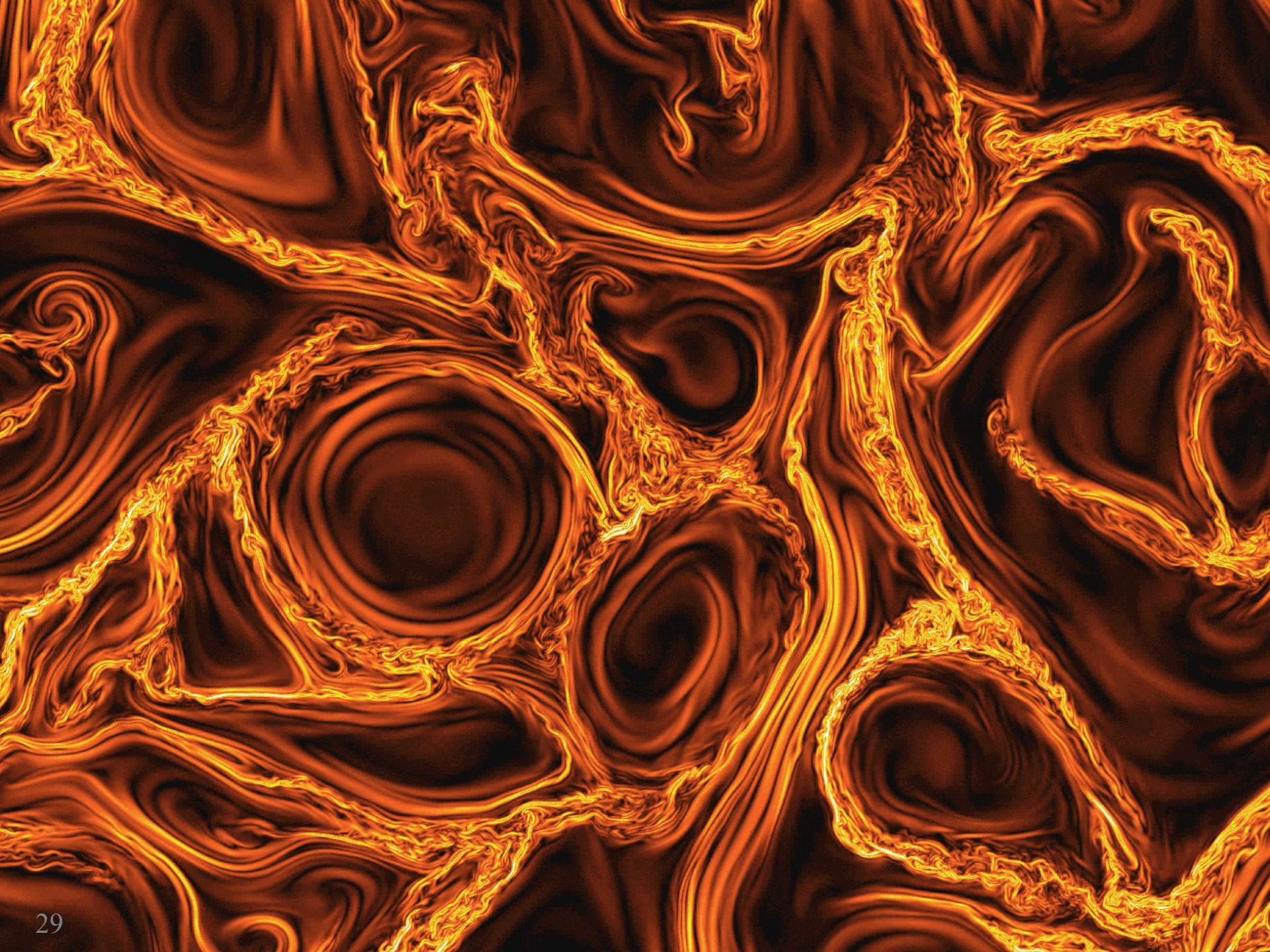
“strong field”



“weak field”

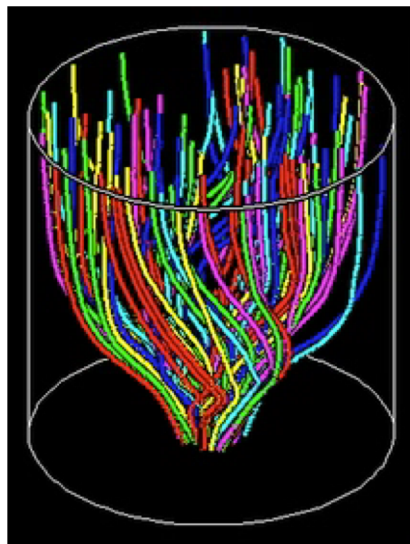
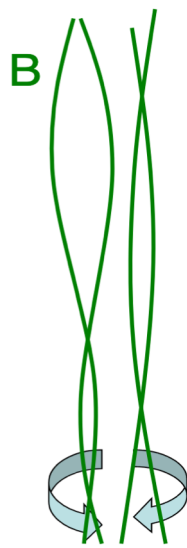
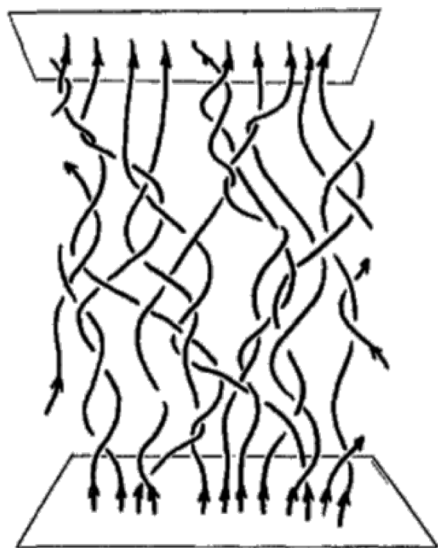
- Wave-packet collisions create higher harmonics (perpendicular to \mathbf{B}).
- Howes (2016) showed that there's a similar behavior as with the addition of harmonics to make a square wave...
- Thin **current sheets** (at which guide-field reconnection occurs) occur naturally at small (kinetic) dissipation scales.



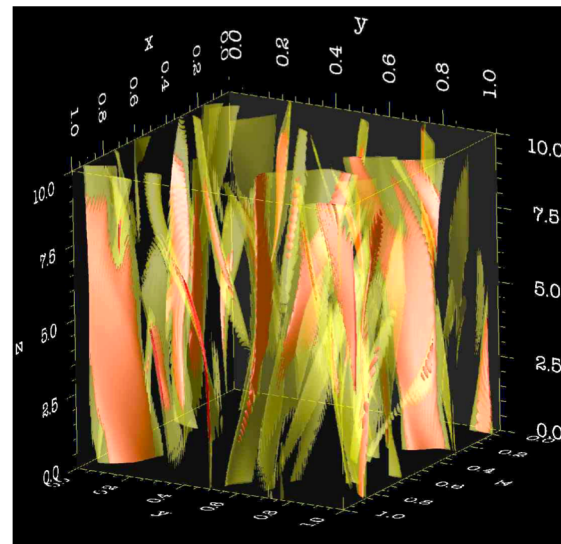


(3) *MHD turbulence and reconnection*

- A snapshot of a current-sheet-filled “box of turbulence” looks pretty much like what Parker (1972, 1983, 1988) had in mind for the tangled/braided DC heating scenario...



van Ballegooijen et al. (2011)



Rappazzo et al. (2007)

- Many models boil down to a cascade rate that's a modification of Kolmogorov's rate:

$$Q_{\text{heat}} \approx \frac{\rho u^3}{\lambda_{\text{ph}}} \left(\frac{\tau_{\text{ph}}}{\tau_A} \right)^q$$

$$q = \begin{cases} 0 & \text{(Kolmogorov 1941)} \\ 1-2 & \text{(Galsgaard \& Nordlund 1996)} \\ 1.5 & \text{(Dmitruk \& Gomez 1999)} \\ 1.5-2 & \text{(Rappazzo et al. 2008)} \\ 2 & \text{(van Ballegooijen 1986; Parker 1988)} \end{cases}$$

$$\begin{aligned} m &= 2 - q \\ n &= 1 \end{aligned}$$

Conclusions

- The **coronal heating problem** is far from being solved, but I hope that we've conveyed some of the relevant physics problems that are involved.
- New observations (higher spatial/time/spectral resolution) are needed!

For next week

- Read paper 3: “Stellar Wind Mechanisms and Instabilities,” a review paper by Stan Owocki (2004). [PDF is here.](#)
- You only need to read **sections 1, 2, and 3** (numbered pages 163–181; i.e., just the first 19 pages of the PDF)
- Participate in the [#paper-3-discussion](#) channel on Slack for next week (February 17, 2022)

